

# Ground and Excited State Dipole Moments of BADAN and ACRYLODAN Determined from Solvatochromic Shifts of Absorption and Fluorescence Spectra

A. Kowski, B. Kukliński, and P. Bojarski

Institute of Experimental Physics, University of Gdańsk, ul. Wita Stwosza 57, PL-80-952 Gdańsk, Poland

Reprint requests to Prof. A. K., ul. Gen. W. Sikorskiego 11, PL-84-200 Wejherowo, Poland

Z. Naturforsch. **56a**, 407–411 (2001); received March 16, 2001

The electric dipole moments in the ground  $\mu_g$  and excited states  $\mu_e$  of the fluorescent probes BADAN (6-bromoacetyl-2-dimethylamino-naphthalene) and ACRYLODAN (6-acryloyl-2-dimethylamino-naphthalene) are determined from the solvatochromic shifts of their absorption and fluorescence spectra for two Onsager interaction radii ( $a = 4.2$  and  $4.6$  Å). The obtained values of  $\mu_g$  and  $\mu_e$  for BADAN are comparable to those of PRODAN, while for ACRYLODAN they are distinctly greater.

**Key words:** Solvatochromic Shifts; Dipole Moments in the Ground and Excited States; BADAN and ACRYLODAN-Fluorescent Probes.

## 1. Introduction

Recently, the interest in the properties of PRODAN-like fluorescent probes has grown because of the enormous difference in the dipole moments  $\mu_e - \mu_g$  of PRODAN between the excited (e) and ground (g) state as a result of optical excitation to the lowest excited singlet state.

For PRODAN, the very high value of  $\mu_e = 20$  D compared to that of  $\mu_g = 2$  D, determined by Macgregor and Weber [1], is incorrect, as shown by Balter et al. [2]. Further work [3–5] demonstrated that the ratio  $\mu_e/\mu_g$  is approximately 3, similarly as for LAURDAN.

Several variants of the original fluorescent PRODAN probe, described by Weber and Farris [6], have later been prepared, including the thiol-reactive derivatives

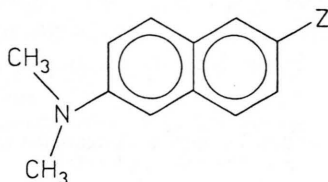
BADAN (6-bromoacetyl-2-dimethylamino-naphthalene) and ACRYLODAN (6-acryloyl-2-dimethylamino-naphthalene), which can be used to transfer the environment – sensitive properties of this fluorophore on bioconjugates. BADAN, PRODAN, and ACRYLODAN show fluorescence that is extremely sensitive to the solvent polarity [6–8].

The present work reports on the effect of different substituents Z (given in Fig. 1) in 2-(dimethylamino)naphthalene on the dipole moment in the ground and excited state.

## 2. Basic Equations for the Analysis of Electric Dipole Moments in the Ground and Excited State

The following equations are based on quantum – mechanical perturbation theory [9, 10] of absorption ( $\tilde{\nu}_A$ ) and fluorescence ( $\tilde{\nu}_F$ ) band shifts (in wavenumbers) in solvents of permittivity  $\epsilon$  and refractive index  $n$ , relative to the band positions of the molecule in the gaseous state. For a spherical molecule, if  $\alpha/a^3 = 1/2$ , where  $\alpha$  is the polarizability and  $a$  the Onsager interaction radius of the solute, one has [11]

$$\Delta \tilde{\nu}_{A,F} = -m_{A,F} \left( \frac{2n^2 + 1}{n^2 + 2} \right) \cdot \left( \frac{\epsilon - 1}{\epsilon + 2} - \frac{n^2 - 1}{n^2 + 2} \right) - m_2 \frac{3}{2} \frac{n^4 - 1}{(n^2 + 2)^2} \quad (1)$$



MOLECULE :	PRODAN	BADAN	ACRYLODAN
Substituent Z :	$\text{CH}_3\text{---CH}_2\text{---C}(=\text{O})$	$\text{Br---CH}_2\text{---C}(=\text{O})$	$\text{CH}_2=\text{CH---C}(=\text{O})$

Fig. 1. Structural formula of PRODAN, BADAN, and ACRYLODAN.

0932-0784 / 01 / 0500-0407 \$ 06.00 © Verlag der Zeitschrift für Naturforschung, Tübingen · www.znaturforsch.com



Dieses Werk wurde im Jahr 2013 vom Verlag Zeitschrift für Naturforschung in Zusammenarbeit mit der Max-Planck-Gesellschaft zur Förderung der Wissenschaften e.V. digitalisiert und unter folgender Lizenz veröffentlicht: Creative Commons Namensnennung-Keine Bearbeitung 3.0 Deutschland Lizenz.

Zum 01.01.2015 ist eine Anpassung der Lizenzbedingungen (Entfall der Creative Commons Lizenzbedingung „Keine Bearbeitung“) beabsichtigt, um eine Nachnutzung auch im Rahmen zukünftiger wissenschaftlicher Nutzungsformen zu ermöglichen.

This work has been digitalized and published in 2013 by Verlag Zeitschrift für Naturforschung in cooperation with the Max Planck Society for the Advancement of Science under a Creative Commons Attribution-NoDerivs 3.0 Germany License.

On 01.01.2015 it is planned to change the License Conditions (the removal of the Creative Commons License condition “no derivative works”). This is to allow reuse in the area of future scientific usage.

Hence, from (1) the following equations are obtained:

$$\tilde{\nu}_A - \tilde{\nu}_F = m_1 f(\varepsilon, n) + \text{const}, \quad (2)$$

$$\tilde{\nu}_A + \tilde{\nu}_F = -m_2 [f(\varepsilon, n) + 2g(n)] + \text{const}, \quad (3)$$

where

$$m_1 = \frac{2(\mu_e - \mu_g)^2}{hca^3}, \quad (4)$$

$$m_2 = \frac{2(\mu_e^2 - \mu_g^2)}{hca^3}, \quad (5)$$

$$m_A = \frac{2\mu_g(\mu_e - \mu_g)}{hca^3}, \quad (6)$$

$$m_F = \frac{2\mu_e(\mu_e - \mu_g)}{hca^3}. \quad (7)$$

The parameters of the solvent polarity are given by

$$f(\varepsilon, n) = \frac{2n^2 + 1}{n^2 + 2} \cdot \left( \frac{\varepsilon - 1}{\varepsilon + 2} - \frac{n^2 - 1}{n^2 + 2} \right), \quad (8)$$

$$g(n) = \frac{3}{2} \frac{n^4 - 1}{(n^2 + 2)^2}. \quad (9)$$

Assuming that the symmetry of the solute molecule remains unchanged on electronic transition and the ground and excited state dipole moments are parallel, together with (4) and (5) one obtains [9, 12]

$$\mu_g = \frac{m_2 - m_1}{2} \left( \frac{hca^3}{2m_1} \right)^{1/2}, \quad (10)$$

$$\mu_e = \frac{m_1 + m_2}{2} \left( \frac{hca^3}{2m_1} \right)^{1/2}. \quad (11)$$

Division of (11) by (10) gives

$$\frac{\mu_e}{\mu_g} = \frac{m_1 + m_2}{m_2 - m_1} = \frac{m_F}{m_A}, (m_2 > m_1), \quad (12)$$

where

$$m_A = \frac{m_2 - m_1}{2}, \quad (13)$$

$$m_F = \frac{m_1 + m_2}{2}. \quad (14)$$

As shown by Baba *et al.* [13], the dipole moments in the excited state in two solvents 1 and 2 which have the same refractive index  $n$  but different permittivities  $\varepsilon$ , can be determined. It follows from (1) that for the relative frequency shift between two different solvents 1 and 2 one has

$$\begin{aligned} \Delta\tilde{\nu}_{A,F} &= \Delta\tilde{\nu}_{A,F}(2) - \Delta\tilde{\nu}_{A,F}(1) \\ &= -m_{A,F} \left( \frac{2n^2 + 1}{n^2 + 2} \right) \cdot \left( \frac{\varepsilon_2 - 1}{\varepsilon_2 + 2} - \frac{\varepsilon_1 - 1}{\varepsilon_1 + 2} \right). \end{aligned} \quad (15)$$

In this case we obtain

$$\frac{\Delta\tilde{\nu}_F}{\Delta\tilde{\nu}_A} = \frac{m_F}{m_A} = \frac{\mu_e}{\mu_g}, \quad (16)$$

an equation which is similar to (12) for parallel  $\mu_g$  and  $\mu_e$ , although their directions may be not the same.

### 3. Experimental

#### 3.1. Materials and Methods

BADAN and ACRYLODAN were purchased from Molecular Probes. The solvents were spectroscopically pure. Absorption and fluorescence spectra were measured with the apparatus described in [14, 15], upon excitation  $\tilde{\nu}_{\text{exc}} = 25641 \text{ cm}^{-1}$  and  $23810 \text{ cm}^{-1}$  for BADAN and ACRYLODAN, respectively.

#### 3.2. Absorption and Fluorescence Spectra of BADAN and ACRYLODAN in Different Solvents

Figures 2 and 3 show selected spectra of BADAN and ACRYLODAN in different solvents, respectively. Among the solvents used only two have approximately the same refraction index:  $n$ -hexane  $n = 1.37499$  ( $g(n) = 0.2531$ ), ethyl acetate  $n = 1.37257$  ( $g(n) = 0.2517$ ), of legends of Figs. 4 and 5. The absorption peaks for BADAN are located in these two solvents at  $\tilde{\nu}_A = 27151 \text{ cm}^{-1}$  and  $\tilde{\nu}_A = 26427 \text{ cm}^{-1}$ , respectively, and the fluorescence peaks at  $\tilde{\nu}_F = 24986 \text{ cm}^{-1}$  and  $\tilde{\nu}_F = 22601 \text{ cm}^{-1}$ , respectively. Similarly, for ACRYLODAN we have:  $\tilde{\nu}_A = 27502 \text{ cm}^{-1}$  and  $\tilde{\nu}_A = 26343 \text{ cm}^{-1}$ , respectively, and  $\tilde{\nu}_F = 24162 \text{ cm}^{-1}$  and  $\tilde{\nu}_F = 19757 \text{ cm}^{-1}$ , respectively.

Figures 4–7 show the spectral shifts  $\tilde{\nu}_A - \tilde{\nu}_F$  and  $\tilde{\nu}_A + \tilde{\nu}_F$  of BADAN and ACRYLODAN in different solvents versus the solvent polarity functions  $f(\varepsilon, n)$  and  $f(\varepsilon, n) + 2g(n)$ , respectively. A linear regression was carried out, and a fit to the data was obtained. The obtained slopes  $m_1$  and  $m_2$  of the fitted lines shown in Figs. 4–7 are given in Table 1.

If the dipole moments  $\mu_g$  and  $\mu_e$  are parallel it is possible, based on (12), to determine the ratio  $\mu_e/\mu_g$  for both molecules studied. For BADAN  $\mu_e/\mu_g = 2.9$  was

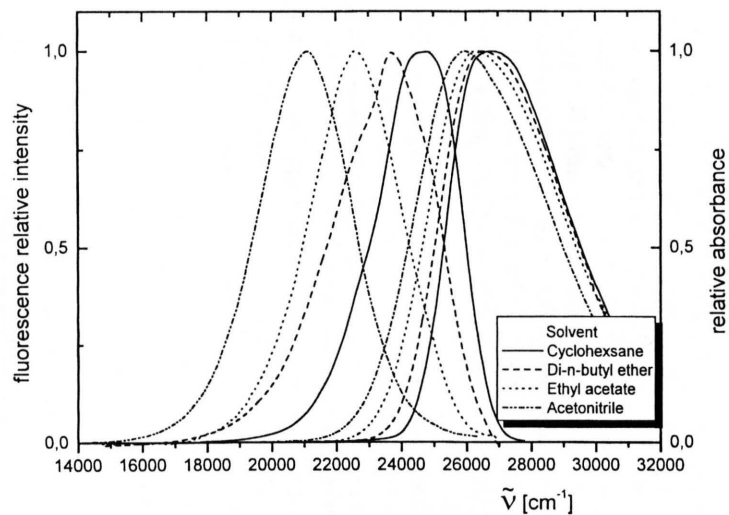


Fig. 2. Absorption and fluorescence spectra of BADAN in different solvents.

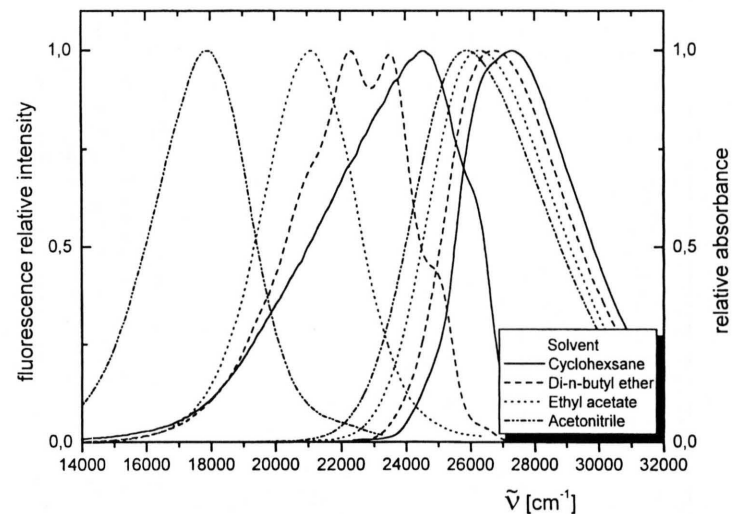
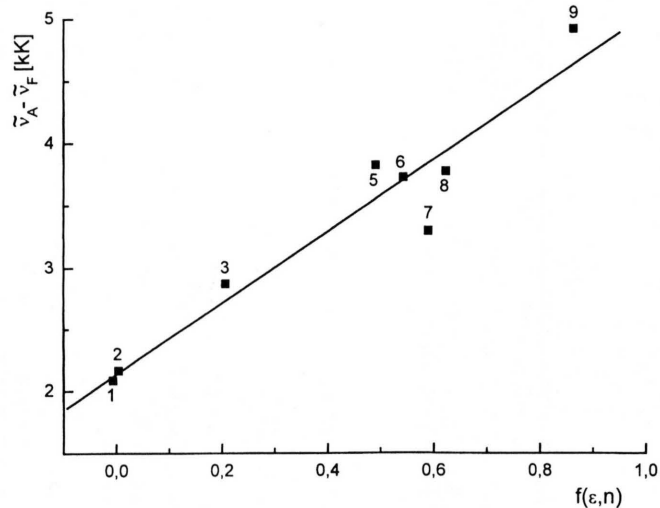
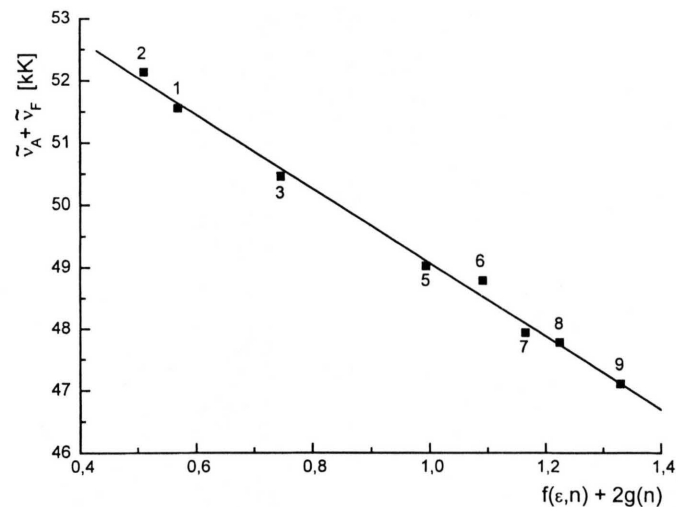


Fig. 3. Absorption and fluorescence spectra of ACRYLODAN in different solvents.

Fig. 4. Plot of  $\tilde{\nu}_A - \tilde{\nu}_F$  versus  $f(\epsilon, n)$  for BADAN in different solvents: 1: cyclohexane, 2: *n*-hexane, 3: di-*n*-butyl ether, 5: ethyl acetate, 6: tetrahydrofuran, 7: 1,2-dichloromethane, 8: 1,2-dichloroethane, 9: acetonitrile.Fig. 5. Plot of  $\tilde{\nu}_A + \tilde{\nu}_F$  versus  $f(\epsilon, n) + 2g(n)$  for BADAN in the same solvents as in Figure 4.

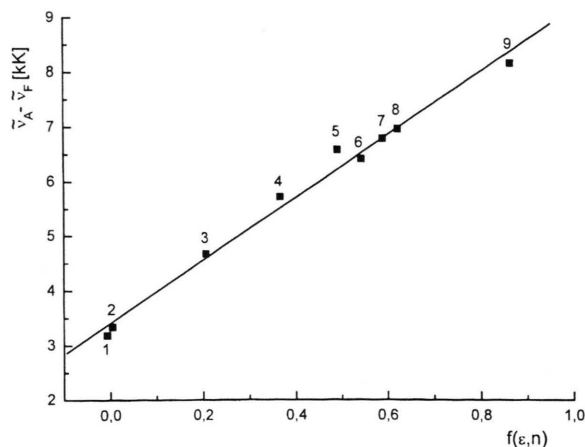


Fig. 6. Plot of  $\tilde{\nu}_A - \tilde{\nu}_F$  versus  $f(\epsilon, n)$  for ACRYLODAN in different solvents: 1: cyclohexane, 2: *n*-hexane, 3: di-*n*-butyl ether, 4: diethylether, 5: ethyl acetate, 6: tetrahydrofuran, 7: 1,2-dichloromethane, 8: 1,2-dichloroethane, 9: acetonitrile.

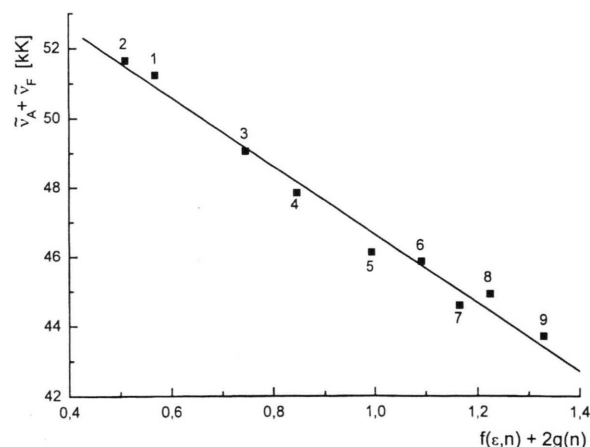


Fig. 7. Plot of  $\tilde{\nu}_A + \tilde{\nu}_F$  versus  $f(\epsilon, n) + 2g(n)$  for ACRYLODAN in the same solvents as in Fig. 6.

obtained, which is close to  $\mu_e/\mu_g$  determined previously for PRODAN [3, 4] (cf. Table 1). However, for ACRYLODAN the higher value  $\mu_e/\mu_g = 3.8$  was obtained.

In the case of BADAN, based on the relative shifts of absorption  $\Delta\tilde{\nu}_A = 724 \text{ cm}^{-1}$  and fluorescence bands  $\Delta\tilde{\nu}_F = 2385 \text{ cm}^{-1}$  according to (16) we obtain  $\Delta\tilde{\nu}_F/\Delta\tilde{\nu}_A = \mu_e/\mu_g = 3.29$ . However, for ACRYLODAN  $\Delta\tilde{\nu}_F/\Delta\tilde{\nu}_A = \mu_e/\mu_g = 3.8$  is obtained. In the latter case the values of  $\mu_e/\mu_g$  determined in two different ways (from (12) and (16)) are equal. For BADAN, however, two dis-

Table 1. Dipole moments of PRODAN, BADAN, and ACRYLODAN determined from solvatochromic shifts of absorption and fluorescence spectra. The conversion factor for the dipole moment:  $[\mu]_{\text{SI}}/\text{Cm} = 3.33564 \times 10^{-30} [\mu]_{\text{cgs}}/D$ , where  $D$  is the symbol of Debye and  $1D = 10^{-18} \text{ esu cm}$ .

Molecule	Onsager radius $a$ [Å]	$\mu_g$	$\mu_e$	$\Delta\mu$	$\mu_e/\mu_g$	$m_1$	$m_2$
		in Debye [D]				[cm <sup>-1</sup> ]	
PRODAN	4.2	2.14	6.43	4.29	3.00	2450	4900
	4.6	2.46	7.37	4.91			
BADAN	4.2	2.44	7.05	4.61	2.9	2895	5950
	4.6	2.79	8.08	5.29			
ACRYLO- DAN	4.2	2.36	8.97	6.61	3.8	5750	9860
	4.6	2.66	10.12	7.46			

tinctly different values for  $\mu_e/\mu_g$  are obtained, based on (12)  $\mu_e/\mu_g = 2.9$  and (16)  $\mu_e/\mu_g = 3.29$ .

#### 4. Ground and Excited State Dipole Moments of BADAN and ACRYLODAN

According to (10) and (11) the dipole moments  $\mu_g$  and  $\mu_e$  depend not only on the parameters  $m_1$  and  $m_2$ , but also on the Onsager interaction radius  $a$ . For BADAN and ACRYLODAN one can assume the same values of  $a$  as for PRODAN (see Fig. 1). Assuming  $a = 4.2 \text{ Å}$ , determined from crystallographic data [6], and  $a = 4.6 \text{ Å}$ , based on the calculation of the spherical cave volume being the sum of all atomic volumes [16], we can calculate  $\mu_g$  and  $\mu_e$  for the values of  $m_1$  and  $m_2$  given in Table 1. The results are also given in Table 1.

The values of  $\mu_g$  and  $\mu_e$  obtained for BADAN differ slightly from those for PRODAN. Comparison of the structural formulae (Fig. 1) leads to the conclusion that the compounds BADAN and PRODAN differ only in the substituents Br and  $\text{CH}_3$ , respectively. However, for ACRYLODAN much higher values of the dipole moments  $\mu_g$  and  $\mu_e$  as well as  $\mu_e/\mu_g = 3.8$  were obtained.

#### 5. Conclusions

The obtained values of  $\mu_g$  and  $\mu_e$  for BADAN (see Table 1) are comparable to those of PRODAN, but for ACRYLODAN they are distinctly greater. The ratio

$\mu_e/\mu_g$  determined by the method of Baba *et al.* [13] for only two solvents with different permittivities  $\epsilon$  and identical refractive indexes  $n$  is completely accidental. Besides, great difficulties are encountered to find solvents which could satisfy this condition. The most reliable values of dipole moments are obtained based on

measurements of absorption and fluorescence band shifts performed in many different solvents with various  $\epsilon$  and  $n$ . For a known value of  $\mu_g$  determined experimentally based on dielectric studies it is possible for parallel  $\mu_g$  and  $\mu_e$  to obtain  $\mu_e$  from (12) without knowing the Onsager radius  $a$ .

- [1] R. B. Macgregor and G. Weber, *Nature (London)* **319**, 70 (1986).
- [2] A. Balter, W. Nowak, W. Pawelkiewicz, and A. Kowalczyk, *Chem. Phys. Letters* **143**, 565 (1988).
- [3] A. Kowski, *Z. Naturforsch.* **54a**, 379 (1999).
- [4] A. Kowski, B. Kukliński, and P. Bojarski, *Z. Naturforsch.* **55a**, 550 (2000).
- [5] A. Kowski, B. Kukliński, P. Bojarski, and H. Diehl, *Z. Naturforsch.* **55a**, 817 (2000).
- [6] G. Weber and F. J. Farris, *Biochem.* **18**, 3075 (1979).
- [7] F. G. Prendergast, M. Meyer, G. L. Carlson, S. Jida, and J. D. Potter, *J. Biol. Chemistry*, **258**, 7541 (1983).
- [8] T. Hiratsuka, *J. Biol. Chem.*, **274**, 29156 (1999).
- [9] L. Bilot and A. Kowski, *Z. Naturforsch.* **17a**, 621 (1962); **18a**, 10 and 256 (1963).
- [10] A. Kowski, *Acta Phys. Polon.* **29**, 507 (1966).
- [11] A. Kowski, *Acta Phys. Polon.* **25**, 285 (1964).
- [12] A. Kowski, *Naturwissensch.* **51**, 82 (1964).
- [13] H. Baba, L. Goodman, and P. C. Valenti, *J. Amer. Chem. Soc.*, **88**, 5410 (1966).
- [14] A. Kowski, G. Piszczek, B. Kukliński, and T. Nowosielski, *Z. Naturforsch.* **49a**, 824 (1994).
- [15] A. Kowski, G. Piszczek, and B. Kukliński, *Z. Naturforsch.* **50a**, 949 (1995).
- [16] W. Nowak, P. Adamczak, A. Balter, and A. Syguła, *J. Mol. Struct. THEOCHEM* **139**, 13 (1986).